

FIN 325 Corporate Finance

L1 (Techniques): Cash Flows and Present Value

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Introduction to cash flows

- The amount of cash moving in/out of the firm.
- A main variable of interest for corporate finance; can be used by the firm to invest or remain solvent.
- Different from accounting items like net income.
 - You can't spend accounting earnings.
 - Ignores earnings that are yet to be received.
 - Cash flows are related to such accounting measures though.
- We treat a firm like a collection of **individual projects**.
- Cash flows arising from a project are treated like cash flows coming from a security, (e.g. a bond).

Time value of money

- Money today is not worth the same as money tomorrow!
- Consider receiving \$1 today. Say you can deposit that \$1 into a bank account and receive interest rate $r\%$ per year.
 - Will be worth $\$(1+r)$ next year.
 - $\$1 \rightarrow \$(1+r)$.
- Now consider receiving \$1 next year.
 - Will be worth $\$X$ today.
 - $\$X \leftarrow \1 .
 - $\$X = \frac{1}{1+r}$.
 - If put $\$\frac{1}{1+r}$ into the bank account for one year, it will give us \$1 next year.
- Notice that $\frac{1}{1+r} < 1$, meaning that \$1 tomorrow is worth less than \$1 today.

Present value: first principles

- First principles definition of present value

$$\begin{aligned}PV_0 &= C_0 + \frac{C_1}{1+r} + \frac{C_2}{(1+r)^2} + \dots + \frac{C_T}{(1+r)^T} \\ &= \sum_{t=0}^T \frac{C_t}{(1+r)^t}\end{aligned}$$

where C_t is the cash flow received at time t .

- T could be **finite** or **infinite**.
- When we assume that $C_t = C$ constant, we get a whole bunch of nice properties.

Present value: perpetuity

- Nice formula for an infinitely-received payment of C

$$\begin{aligned}PV_0 &= \sum_{t=1}^{\infty} \frac{C}{(1+r)^t} \\ &= \frac{C}{1+r} + \frac{C}{(1+r)^2} + \frac{C}{(1+r)^3} + \dots \\ &= \frac{C}{r}\end{aligned}$$

- Derivation

$$\begin{aligned}(1+r)PV_0 &= (1+r) \left[\frac{C}{1+r} + \frac{C}{(1+r)^2} + \frac{C}{(1+r)^3} + \dots \right] \\ &= C + \frac{C}{1+r} + \frac{C}{(1+r)^2} + \frac{C}{(1+r)^3} + \dots \\ \Rightarrow (1+r)PV_0 - PV_0 &= C \\ \Rightarrow PV_0 &= \frac{C}{r}\end{aligned}$$

Present value: growing perpetuity

- Start with a payment of \$C tomorrow and grow forever at a rate of g .

$$PV_0 = \frac{C}{r - g}$$

- Derivation: exercise!

Present value: annuities

- Start with a payment of \$C tomorrow and receive it for T years.

$$\begin{aligned}PV_0 &= \sum_{t=1}^T \frac{C}{(1+r)^t} \\ &= \frac{C}{r} \left[1 - \frac{1}{(1+r)^T} \right]\end{aligned}$$

- Derivation: the difference of two perpetuities.

$$\begin{aligned}PV_0 &= \left[\frac{C}{1+r} + \dots + \frac{C}{(1+r)^T} + \dots \right] - \left[\frac{C}{(1+r)^{T+1}} + \dots \right] \\ &= \frac{C}{r} - \frac{1}{(1+r)^T} \left[\frac{C}{1+r} + \dots + \frac{C}{(1+r)^T} + \dots \right] \\ &= \frac{C}{r} - \frac{1}{(1+r)^T} \frac{C}{r} \\ &= \frac{C}{r} \left[1 - \frac{1}{(1+r)^T} \right]\end{aligned}$$

Present value: growing annuities

- Start with a payment of \$C tomorrow and receive it for T years; grows at rate g between years.

$$\begin{aligned}PV_0 &= \sum_{t=1}^T \frac{C(1+g)^{t-1}}{(1+r)^t} \\ &= \frac{C}{r-g} \left[1 - \frac{(1+g)^T}{(1+r)^T} \right]\end{aligned}$$

- Derivation: same idea as with $g = 0$.

Inflation and discounting (1)

- A rise in the general price level in the economy.



- Nominal value in 1988 — \$70,000 (AUD).
- Nominal value in 2016 — \$1,000,000 (AUD).
- 1 AUD \approx 0.72 USD (Feb. 2016).

Inflation and discounting (2)

- Real rate (r_r): after removing inflation.
- Nominal rate (r_n): unadjusted for inflation.
- The Fisher equation

$$(1 + r_n) = (1 + r_r)(1 + i)$$

- Must use **real discount rate** to discount **real cash flows**.
- Must use **nominal discount rate** to discount **nominal cash flows**.

Finance v.s. accounting (earnings v.s. cash flows)

- Net income is an accounting measure that can be manipulated.
 - E.g. not necessarily one correct way of writing-down depreciation expenses.
- Cash flows are less easy to manipulate.
 - Cash doesn't lie!
- Our approach will be to **start** with reported earnings and make certain adjustments until we get a measure of cash flows.

Defining cash flows (1)

- Main components of free cash flows:
 - Revenues, costs, investments and taxes.
- Depreciation is not a cash flow.
 - Affects taxes though, which are a cash flow.
- Assume for now that the firm is financed entirely with equity.
 - Means no interest expense yet.
- When evaluating a new project, we only care about **incremental** cash flows.
 - Rational agents only think at the margin.
 - **Marginal** benefit versus **marginal** cost.

Defining cash flows (2)

- Definition of cash flows (CF)

$$\begin{aligned} \text{CF} &= (\text{Revenue} - \text{Costs} - \text{Depreciation}) \times (1 - \tau^C) + \text{Depreciation} \\ &\quad - \text{CapEX} - \Delta\text{NWC} \\ &= (\text{Revenue} - \text{Costs}) \times (1 - \tau^C) - \text{CapEX} - \Delta\text{NWC} + \\ &\quad (\tau^C) \times \text{Depreciation} \end{aligned}$$

- Notice I've **added** depreciation back into the earnings since it's not a cash flow.
- Net working capital (NWC) is basically a measure of liquid assets that the firm can use in the short-term.
 - E.g. you expect high demand for your product next week so you invest more in inventories — cash outflow.

$$\begin{aligned} \text{NWC} &= \text{current assets} - \text{current liabilities} \\ &= \text{inventories} + \text{accounts receivable} - \text{accounts payable} \end{aligned}$$

Defining cash flows (3)

- Consider the following example, (with no taxes or NWC).

Year	2016	2017	2018
Revenues	0	550	550
Costs	0	0	0
Depreciation	0	500	500
Net income	0	50	50
CapEx	1000	0	0
FCF	-1000	550	550

- When would we see a scenario with **positive net income** yet **negative CF**?
 - Financial mismanagement (e.g. poor management of NWC).
 - Rapid growth, (e.g. lots of capital expenditures).

Income statement v.s. cash flow statement

- We can relate CF to earnings measures.
- $CF = EBIAT + \text{Depreciation} - \text{CapEx} - \Delta \text{NWC}$.
- $EBIAT = (\text{Revenues} - \text{Costs} - \text{Depreciation}) \times (1 - \tau^C)$.
- $\text{Net income} = EBIAT - (\text{Interest}) \times (1 - \tau^C)$.

Costs

- CapEx (capital expenditures) versus OpEx (operating expenditures).
 - CapEx is investment spending on things that will generate us benefits in the future.
 - OpEx is incurred through day-to-day operations of the company; direct spending on things like wages, utilities or maintenance.
 - OpEx directly enters earnings expressions; CapEx does not.
- Selling, General and Administrative (SG&A).
 - Sales, management and administration costs.
 - Can be looked at as measure of corporate waste.

Sunk costs and decision making

- Sunk costs should be **ignored!**
- Your current and future decision-making doesn't affect these, so they shouldn't be taken into consideration.
- E.g. say you really want to go to Freakfest.
 - You bought your ticket days ago.
 - But you lost it!
 - It is annoying.
 - But if you really want to go, you should buy another ticket, (the lost ticket's purchase cost is sunk).
 - If you keep losing your ticket you should keep buying a new one!

Terminal value

- You're trying to evaluate a potential project.
- How do you treat the project at the horizon's end?
- **Liquidation method:** assumes that you will sell the project at the end; salvage value.
- **Perpetuity method:** assumes that the project will continue indefinitely; continuation value.

Liquidation method (1)

- You'll need an estimate of the project's resale value **after** the final forecast cash flow.
 - Can't sell the project before you're finished using it!
- The market value/selling price of the project relative to the accounting book value will have implications for taxes.
 - Selling price $>$ book value \Rightarrow capital gains \Rightarrow positive taxes!
 - Selling price $<$ book value \Rightarrow capital losses \Rightarrow negative taxes!
- Book value = purchase price - accumulated depreciation

Liquidation method (2)

- Consider the following example.
 - Assume that the project initially cost \$200 in 2016.
 - Say the sale value is \$50.
 - Assume a corporate tax rate of 35%.

	2016	2017	2018	2019	2020
CF excluding terminal value	-200	70	70	70	70
Depreciation	0	4	4	4	4
Accumulated depreciation	0	4	8	12	16
Book value	200	196	192	188	184
Sale value	N/A	N/A	N/A	N/A	50
Tax obligations from termination	N/A	N/A	N/A	N/A	-46.9
Total CF	-200	70	70	70	166.9

- The tax obligation is found as $(0.35) \times (50 - 184)$.
- Total CF is CF excluding TV plus sale value minus tax obligations.

Perpetuity method (1)

- This method assumes that the project will continue forever into the future, (beyond the forecastable future).
- Often also referred to as continuation (rather than terminal) value.
- Our growing perpetuity formula comes in handy here!
- We can apply the growing perpetuity formula to the cash flows realised at the last period in our forecast model.

Perpetuity method (2)

- Consider the following example.
 - Assume that the project will grow at a rate of 2% per year from 2021 onwards.
 - Growth will be applied to **incremental** cash flows.
 - Assume 4% discount rate.

	2016	2017	2018	2019	2020
CF excluding terminal value	-200	70	70	70	70
Continuation value (CV)	N/A	N/A	N/A	N/A	3470
Total CF	-200	70	70	70	3640

- Continuation value = $\frac{70(1.02)}{0.04-0.02}$.
- Total CF = CF excluding TV + CV.
- The continuation value is usually incurred at the **end** of the final period in the forecast model as above.

Takeaways

- Cash flows are our main object of interest.
- They are not the same as accounting earnings.
- Only look at **incremental** cash flows.
- Ignore sunk costs.
- Terminal values can be found using liquidation or perpetuity methods.
- House prices in Melbourne are damn expensive!